# **Progress Toward Standards**

**Grade 7** 

**Mathematics** 

**Framework** 

### **Strand 1: Numbers and Operations**

#### Standard 1.1: Students demonstrate understanding of number concepts.

In the grade 7 test, understanding is demonstrated with the following indicators as well as by solving problems, reasoning, communicating, representing, and making connections based on the indicators—

- translating among forms for expressing large numbers, including scientific notation
- interpreting positive integral exponents and square roots
- interpreting the meanings of proportions and percents, including percents less than 1% and greater than 100%, in real-life situations
- recognizing the relationships among ratios, proportions, and percents
- recognizing and generating equivalent fractions, decimals, and percents
- ordering rational numbers and square roots
- using positive and negative integers to represent real life situations
- reasoning with regard to multiples, factors, primes, and divisibility

# Standard 1.2: Students demonstrate an understanding of the concepts of operations.

In the grade 7 test, understanding is demonstrated with the following indicators as well as by solving problems, reasoning, communicating, representing, and making connections based on the indicators—

- judging the effects of addition, subtraction, multiplication, and division on rational numbers as well as the effects of operations with exponents and square roots
- applying the commutative, associative, identity, inverse, and distributive properties

#### Standard 1.3: Students demonstrate fluency in computing and estimating.

In the grade 7 test, fluency is demonstrated with the following indicators as well as by solving problems, reasoning, communicating, representing, and making connections based on the indicators—

- applying correct order of operations
- adding, subtracting, multiplying, and dividing with whole numbers, fractions, decimals, and integers
- computing with ratios, proportions, and percents
- estimating based on operations described above

### Strand 2: Algebra

### Standard 2.1: Students demonstrate understanding of patterns, relations, and functions.

In the grade 7 test, understanding is demonstrated with the following indicators as well as by solving problems, reasoning, communicating, representing, and making connections based on the indicators—

- representing rules for real life and mathematical linear patterns using words, algebraic expressions, or equations
- drawing conclusions and making predictions based on patterns and relationships, both mathematical and from real life

# Standard 2.2: Students demonstrate the ability to use algebraic symbols to represent and analyze situations.

In the grade 7 test, understanding is demonstrated with the following indicators as well as by solving problems, reasoning, communicating, representing, and making connections based on the indicators—

- representing linear real life situations with algebraic expressions or equations
- solving linear equations in one variable with non-negative integral solutions
- evaluating expressions for given values, e.g., geometric or measurement formulas or in expressions representing real life situations
- recognizing the equivalence of expressions as they relate to the same real life situation
- recognizing the relationship between linear equations and their graphs

### Standard 2.3: Students demonstrate the ability to create models to represent mathematical relationships.

In the grade 7 test, ability is demonstrated with the following indicators as well as by solving problems, reasoning, communicating, representing, and making connections based on the indicators—

• recognizing and creating multiple representations (e.g., words, charts, algebraic expressions or equations, and graphs) of the same linear real life situation

### Standard 2.4: Students demonstrate an understanding of change in a variety of situations.

In the grade 7 test, understanding is demonstrated with the following indicators as well as by solving problems, reasoning, communicating, representing, and making connections based on the indicators—

- matching a situation involving a constant or variable rate of change to a graph that best represents that situation
- determining in a real life situation involving a constant rate of change how a change in one variable affects the other variable

### **Strand 3: Geometry**

# Standard 3.1: Students demonstrate understanding of two- and three-dimensional geometric shapes and the relationships among them.

In the grade 7 test, understanding is demonstrated with the following indicators as well as by solving problems, reasoning, communicating, representing, and making connections based on the indicators—

- reasoning about geometric figures and the relationships among them based on their definitions and properties
- determining characteristics of and relationships among various types of triangles and angles, including vertical, complementary, and supplementary angles
- determining similarity of geometric figures based on congruence of angles and proportionality of sides

### Standard 3.2: Students demonstrate understanding of coordinate systems.

In the grade 7 test, understanding is demonstrated with the following indicators as well as by solving problems, reasoning, communicating, representing, and making connections based on the indicators—

- using ordered pairs as coordinates of points in a four-quadrant coordinate plane
- making connections between properties of geometric figures and coordinate geometry, e.g., given the coordinates of three vertices of a square, finding the coordinates of the fourth vertex

### Standard 3.3: Students demonstrate understanding of symmetry and transformations.

In the grade 7 test, understanding is demonstrated with the following indicators as well as by solving problems, reasoning, communicating, representing, and making connections based on the indicators—

- describing in words the transformation (translation, reflection, or rotation) that moves a figure from one position to another
- determining an image of a figure on the coordinate plane after a translation or reflection
- recognizing the connections between transformations and congruence, line symmetry, and rotational symmetry

# Standard 3.4: Students demonstrate an ability to perform visual and spatial reasoning.

In the grade 7 test, ability is demonstrated with the following indicators as well as by solving problems, reasoning, communicating, representing, and making connections based on the indicators—

- constructing a net (pattern) for a common 3-dimensional figure such as a prism or pyramid
- identifying views (e.g., front, top, right side) of a 3-dimensional structure

#### **Strand 4: Measurement**

# Standard 4.1: Students demonstrate understanding of concepts and processes of measurement.

In the grade 7 test, understanding is demonstrated with the following indicators as well as by solving problems, reasoning, communicating, representing, and making connections based on the indicators—

- selecting the best measurement strategy to use relative to the purpose of the measurement and its required accuracy
- identifying the range of possible "true" measurements, given a measurement with its greatest possible error
- using formulas to determine how a change in side length (radius) or height affects the perimeter (circumference) and area in triangles, parallelograms and circles, and the volume in rectangular and triangular prisms.
- performing conversions among measurements of area and volume, e.g., 1 square centimeter is equal to 100 square millimeters
- predicting how a change in one of the measures of side lengths, perimeters, and areas affect the other of these measurements in a triangle, square, or rectangle
- estimating equivalent measures between the customary and the metric systems based on benchmark equivalents
- making reasonable estimates of distance or height based on common benchmarks
  or given information, e.g., an estimate of the height of tree given a picture of a
  man standing next to the tree

# Standard 4.2: Students demonstrate facility with the tools, procedures, and formulas of measurement.

In the grade 7 test, understanding is demonstrated with the following indicators as well as by solving problems, reasoning, communicating, representing, and making connections based on the indicators—

- estimating perimeters and areas of irregular regions
- solving problems involving rates and common derived measurements, e.g., miles per gallon and cost per unit
- finding perimeters of polygons and, given the formula, circumferences of circles
- using given formulas to find the areas of rectangles, triangles, parallelograms, trapezoids, and circles as well as figures that can be subdivided into these shapes
- using given formulas to find the volumes of prisms, cylinders, cones, and pyramids
- solving problems involving scale factors, e.g., maps and enlargements made with a photocopier
- solving problems involving proportionality and geometric similarity

### **Strand 5: Data Analysis and Probability**

### Standard 5.1: Students demonstrate facility in collecting, organizing, and displaying data.

In the grade 7 test, facility is demonstrated with the following indicators as well as by solving problems, reasoning, communicating, representing, and making connections based on the indicators—

- determining appropriate data to collect for a given purpose and how to go about collecting and analyzing that data
- selecting appropriate graphic representations for data sets
- interpreting and constructing bar graphs, pictographs, line graphs, line plots, stem-and-leaf graphs, circle graphs, frequency charts, histograms, and box-and-whisker graphs
- recognizing how different representations of the same data set can affect interpretation

#### Standard 5.2: Students demonstrate an understanding of statistical methods.

In the grade 7 test, understanding is demonstrated with the following indicators as well as by solving problems, reasoning, communicating, representing, and making connections based on the indicators—

- calculating the mean, median, mode, and range of a data set and interpreting their meanings relative to the data set
- making judgments regarding the shape and spread of data sets, including consideration of outliers and quartiles

# Standard 5.3: Students demonstrate the ability to draw conclusions and make inferences based on data.

In the grade 7 test, ability is demonstrated with the following indicators as well as by solving problems, reasoning, communicating, representing, and making connections based on the indicators—

 drawing conclusions and making inferences and predictions based on data given in charts and graphs

#### Standard 5.4: Students demonstrate an understanding of probability.

In the grade 7 test, understanding is demonstrated with the following indicators as well as by solving problems, reasoning, communicating, representing, and making connections based on the indicators—

- determining all possible outcomes for an experiment, using a tree diagram, an organized list, or, when appropriate, the fundamental counting principle
- finding the theoretical probability of a event in experiment with equally likely outcomes
- finding theoretical probability involving simple independent events
- finding the empirical probability of an event, given a set of data
- making predictions based on probability